

1.2. STOCHASTIC PROCESSES

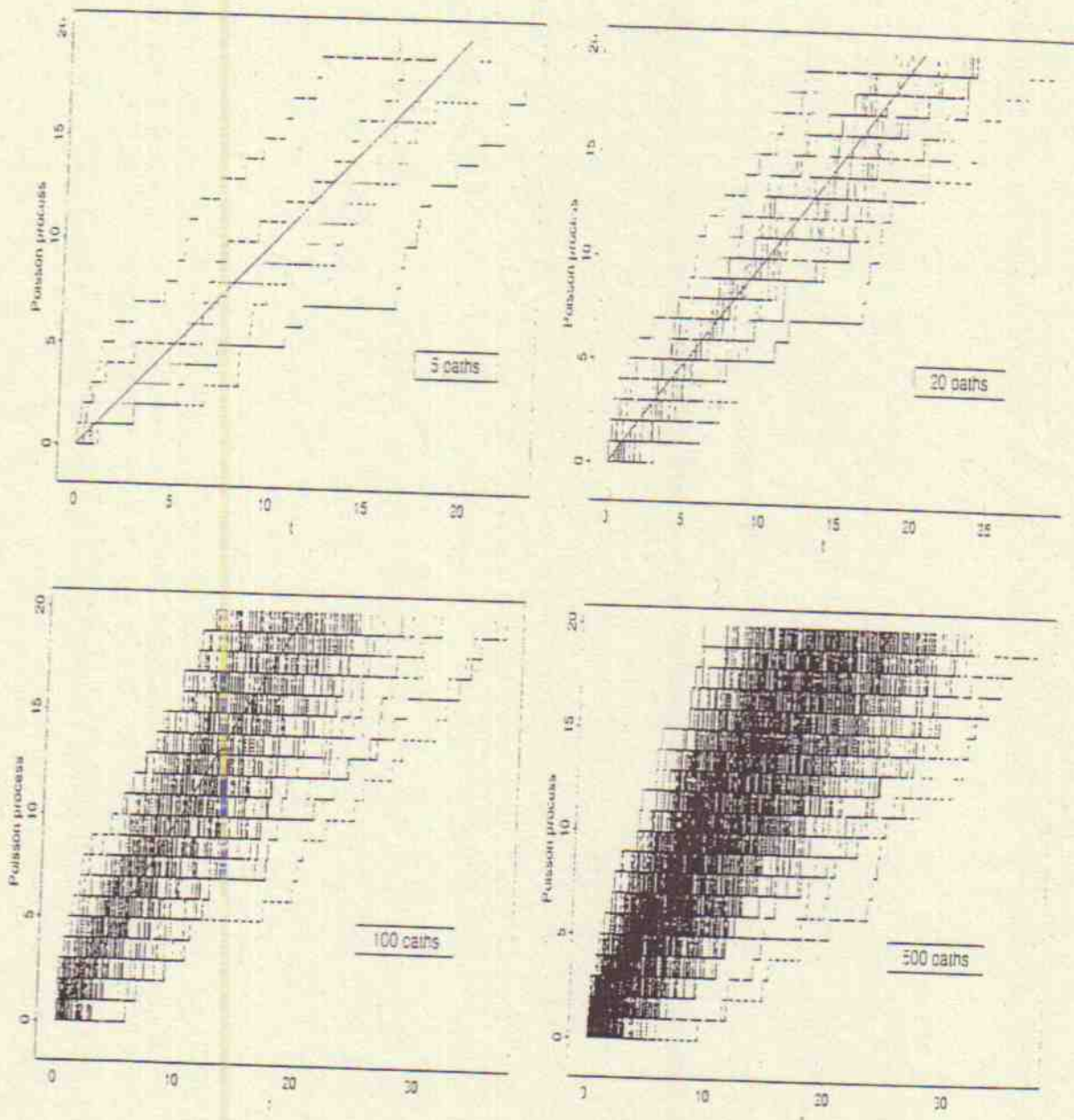


Figure 1.2.9 Sample paths of a homogeneous Poisson process  $(X_t, t \in [0, \infty))$  with intensity  $\lambda = 1$ ; see Example 1.2.10. The straight solid line stands for the expectation function  $\mu_X(t) = t$ .

$(\lambda \hat{=} c)$

$$X_t - \lambda t \quad (\lambda \leq c)$$

(5)

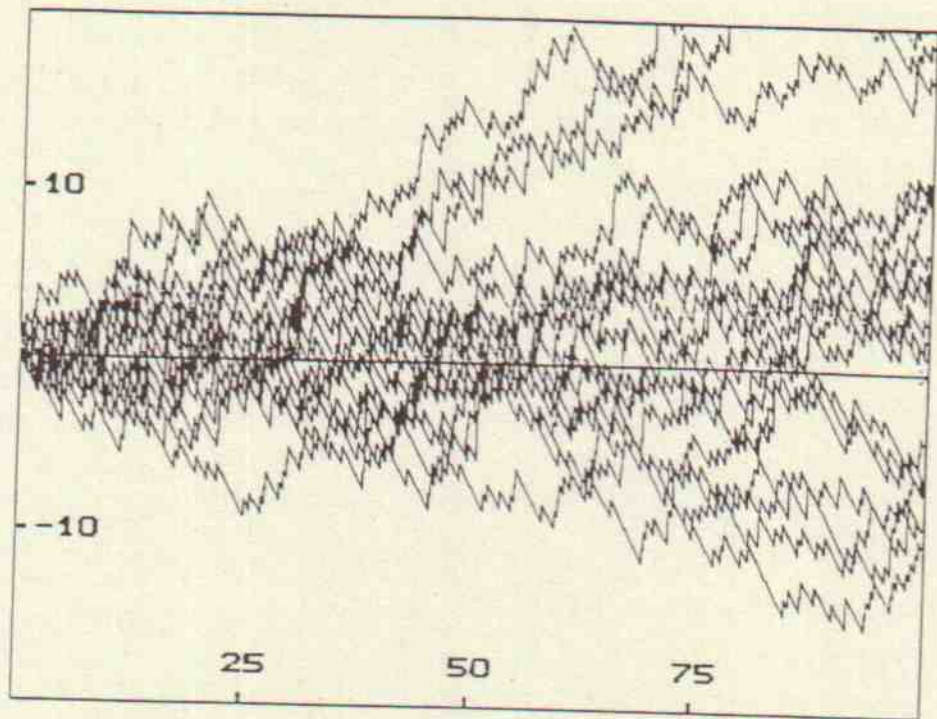


Figure 2.3.1. Trajectories of the Poisson process with compensator for  $\lambda = 1.0$ .

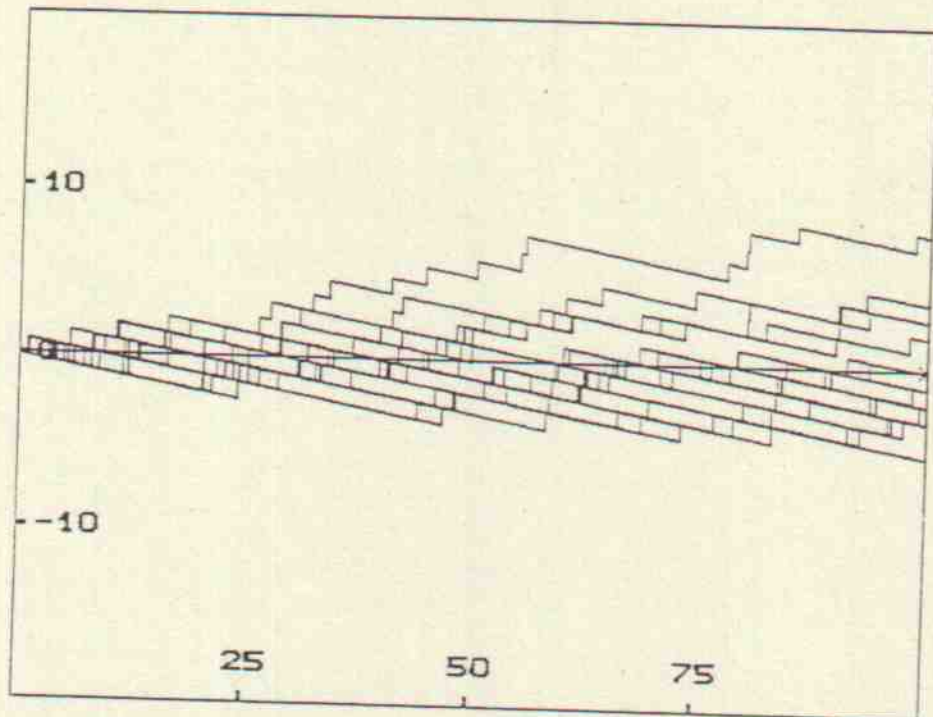


Figure 2.3.2. Trajectories of the Poisson process with compensator for  $\lambda = 0.1$ .

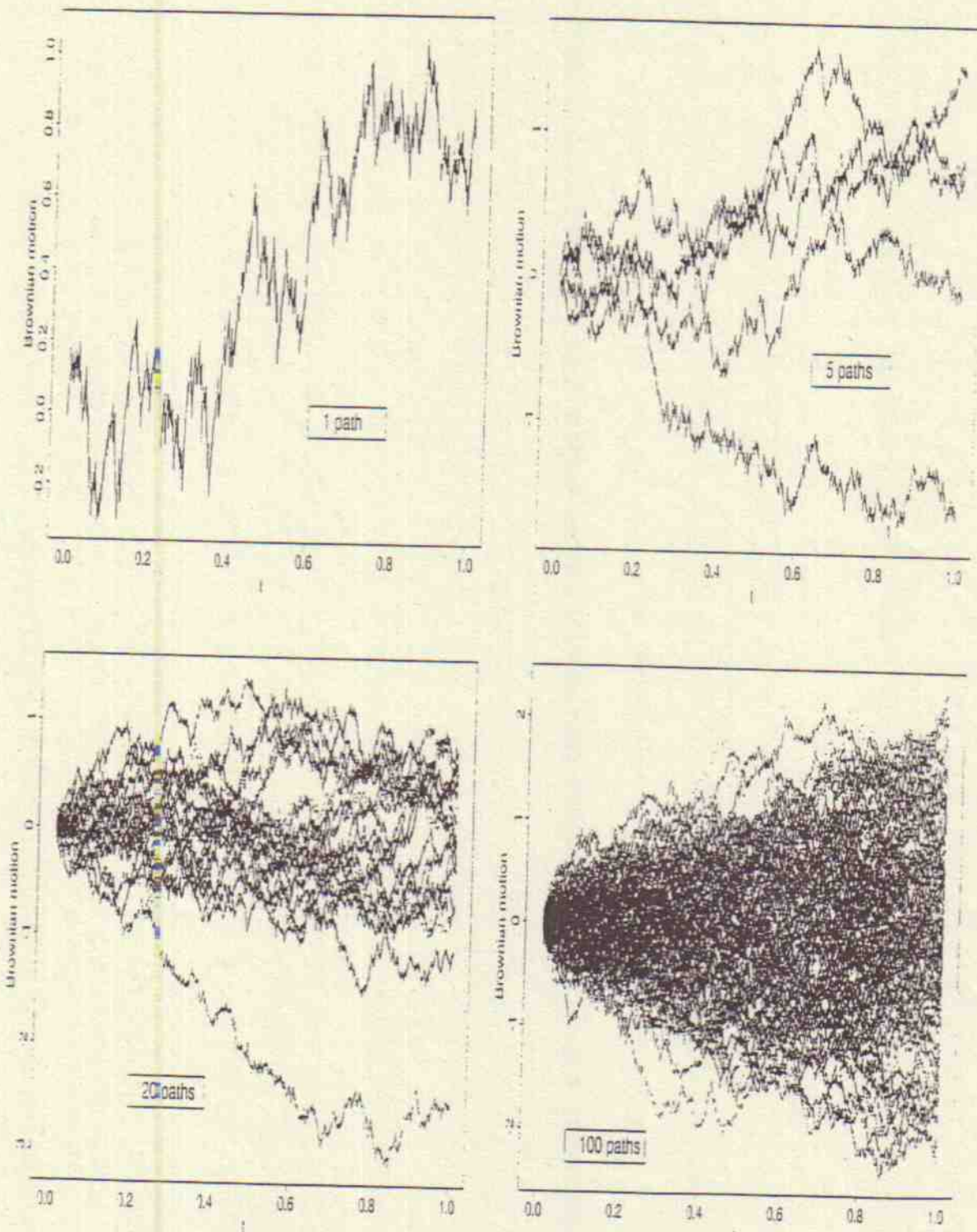


Figure 1.3.1 Sample paths of Brownian motion on  $[0, 1]$ .

BROWNIAN MOTIONS

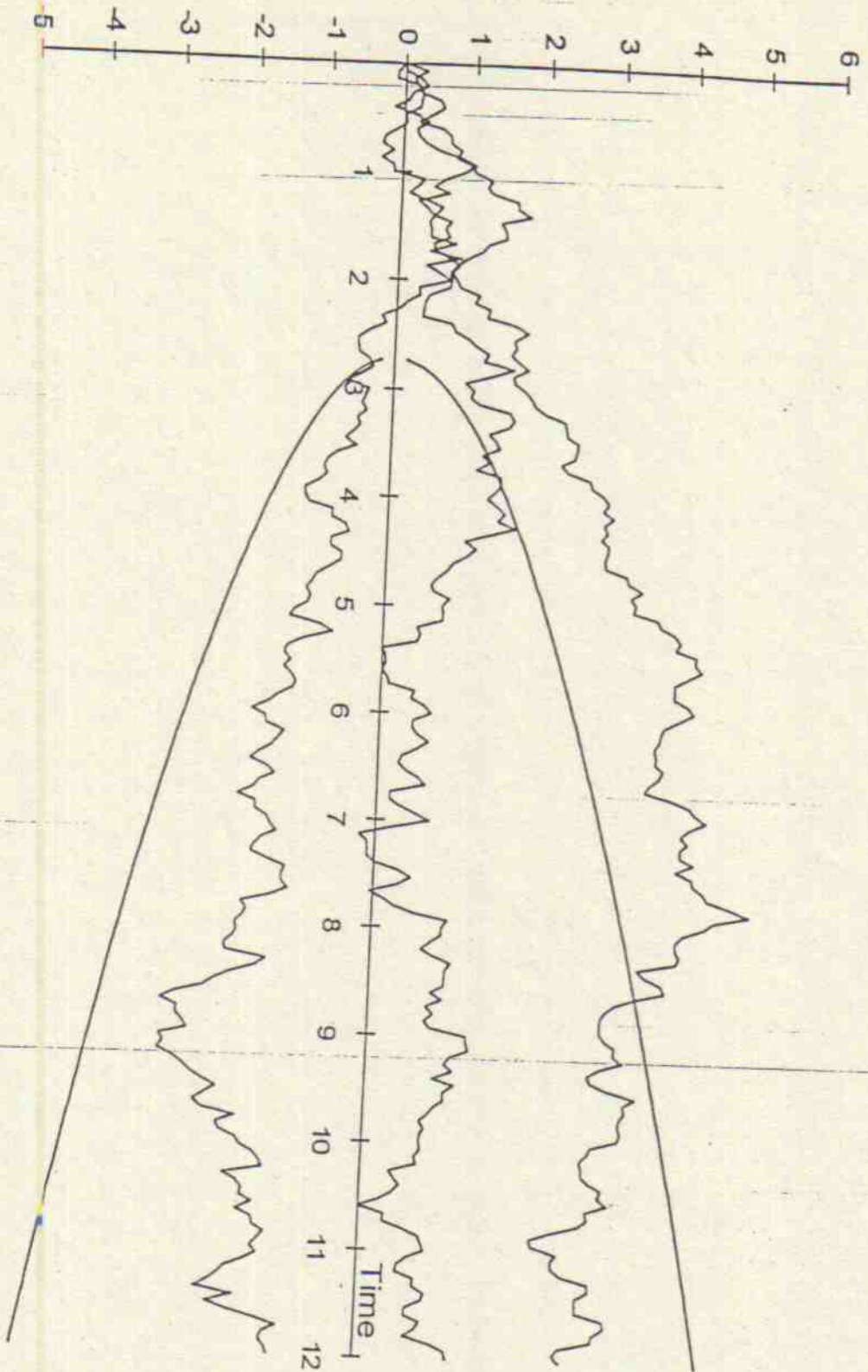


FIG. 1.3. The law of the iterated logarithm

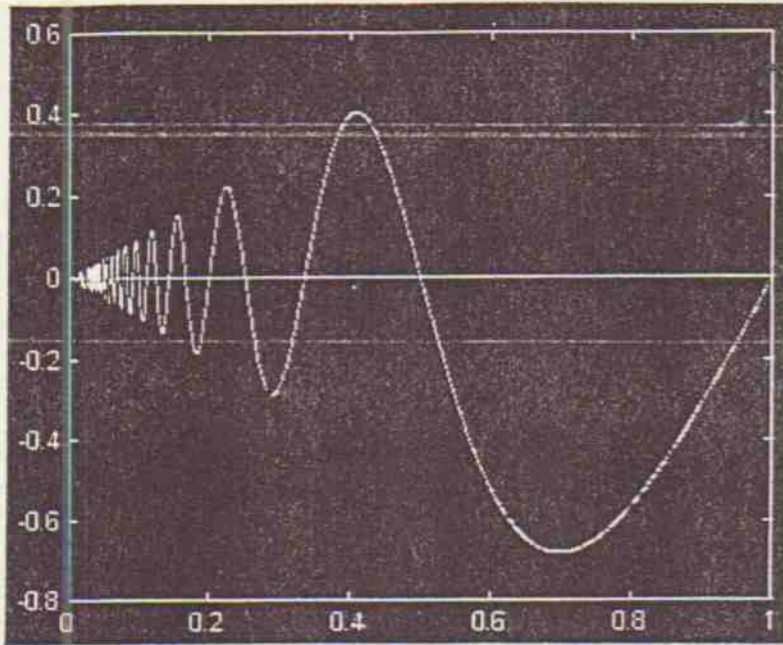


FIGURE 2

3.2.4 An Example

Consider the function

$$f(t) = \begin{cases} t \sin\left(\frac{\pi}{t}\right) & \text{when } 0 < t \leq 1 \\ 0 & \text{when } t = 0 \end{cases} \quad (17)$$

It can be shown that  $f(t)$  is not of bounded variation.<sup>6</sup>